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$$\int x^n dx =$$

$$\frac{x^{n+1}}{n+1} + C$$

$$\int \frac{x^5 + 2x^2 - 1}{x^4} dx$$

No magic
What do
you
know?

$$\begin{aligned} &= \int \frac{x^5}{x^4} dx + \int \frac{2x^2}{x^4} dx - \int \frac{1}{x^4} dx \\ &= \int x dx + 2 \int x^{-2} dx - \int x^{-4} dx \\ &= \frac{x^2}{2} + 2\left(-\frac{1}{x}\right) - \left(-\frac{1}{3}x^{-3}\right) + C \end{aligned}$$

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A
CLASSIC!This is
for You
Justina!

$$\int \sec x (\sec x + \tan x) dx$$

$$= \int \sec^2 x dx + \int \sec x \tan x dx$$

$$= \tan x + \sec x + C$$

$$\begin{aligned} \underline{62/24} \quad & \int \sec x (\tan x + \cos x) dx \\ &= \int \sec x \tan x dx + \int \sec x \cos x dx \\ &= \sec x + \int \frac{1}{\cos x} (\cos x) dx \\ &= \sec x + \int 1 dx = \sec x + x + C \end{aligned}$$

6.3 Integration by Substitution

aka "Integration meets the chain rule"
Justina-note
"also known as"

what is the derivative of $\sin(x^3)$?

$$\frac{d}{dx}(\sin(x^3)) = \cos(x^3)(3x^2)$$

$$\text{so } \int 3x^2 \cos(x^3) dx = \sin(x^3) + C$$

6.3 - integration by substitution

Find

$$\int 3x^2 \cos(x^3) dx$$

if you don't see the answer right away.

Recall the chain rule

$$\frac{d}{dx}(f(g(x))) = f'(g(x)) \cdot g'(x)$$

$$\text{so } \int f'(g(x)) \cdot g'(x) dx = f(g(x)) + C$$

integration
by
substitution:

$$\int f'(g(x)) g'(x) dx$$

$$\text{Let } u = g(x)$$

$$\frac{du}{dx} = g'(x)$$

$$du = g'(x) dx$$

THEN replace " $g'(x) dx$ " in the original ONCE with " du "

AND replace EVERY " $g(x)$ " with " u "

$$\Rightarrow \int f'(u) du = f(u) + C$$

$$= f(g(x)) + C$$

replace u with $g(x)$

u will be a function I treat as a new variable

Convert to differential talk

$$\int \underline{3x^2} \cos(x^3) \underline{dx}$$

$$\text{Let } u = x^3$$

$$\frac{du}{dx} = 3x^2$$

$$\Rightarrow \boxed{du} = \boxed{3x^2 dx}$$

$$\Rightarrow \int \cos(u) du = \sin u + C = \sin(x^3) + C$$

Think 2 yourself:
I know
 $\int \cos u du$

Think of (for now)

$\int (\quad) dx$ as calculus parentheses

$\int 2x (x^2+1)^{50} dx$

Let $u = x^2 + 1$
 $\frac{du}{dx} = 2x$
 $du = 2x dx$

$\Rightarrow \int u^{50} du = \frac{u^{51}}{51} + C = \frac{(x^2+1)^{51}}{51} + C$

L I A T E
 In
 intere-
 tris
 algebraic
 frig
 exponential